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Thermodynamic and kinetic analysis of sensitivity amplification in biological signal transduction

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Abstract

Based on a thermodynamic analysis of the kinetic model for the protein phosphorylation–dephosphorylation cycle, we study the ATP (or GTP) energy utilization of this ubiquitous biological signal transduction process. It is shown that the free energy from hydrolysis inside cells, ΔG (phosphorylation potential), controls the amplification and sensitivity of the switch-like cellular module; the response coefficient of the sensitivity amplification approaches the optimal 1 and the Hill coefficient increases with increasing ΔG . We discover that zero-order ultrasensitivity is mathematically equivalent to allosteric cooperativity. Furthermore, we show that the high amplification in ultrasensitivity is mechanistically related to the proofreading kinetics for protein biosynthesis. Both utilize multiple kinetic cycles in time to gain temporal cooperativity, in contrast to allosteric cooperativity that utilizes multiple subunits in a protein.

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1. Introduction

Biological signal transduction processes are increasingly being understood in quantitative and modular terms [1,2]. One of the most commonly studied modules of cellular ‘circuitry’ is the phosphorylation–dephosphorylation cycle (PdPC) [3] which has been shown to exhibit sensitivity amplification for the appropriate stimuli expressed through activating a kinase or inhibiting a phosphatase [4–6]. Both experimental measurement [7–9] and theoretical modeling have shown that the covalent modification gives rise to a switch-like behavior.

Sensitivity amplification requires energy consumption [4,7,10]. Since the PdPC involves the transfer of high-energy phosphate group, it is natural to ask how the cellular phosphoenergetics play a role in signal transduction processes. Recently, a novel mechanism has been proposed [11] for improved Rab 5 GTPase function as a cellular timer [12] by utilizing the energy derived from GTP hydrolysis. It is shown that energy expenditure is necessary for a GTPase timer to be accurate and robust.

Phosphoenergetics and ATP hydrolysis are also involved in PdPC. While it is known that energy expenditure is required to maintain levels of phosphorylation in excess of an equilibrium [4,10], it is still not clear how cellular energetics relates to this type of signal transduction process. One

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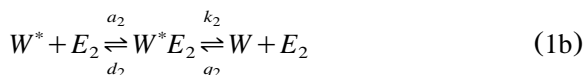
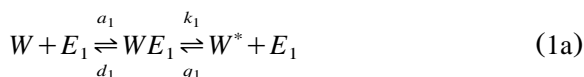
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approach to address this question is to introduce a rigorous thermodynamic analysis into the kinetic models of PdPC [5,8]. The simplest kinetic scheme for PdPC is shown in Eqs. (1a) and (1b), which is based on a model proposed by Stadtman and Chock [4] and by Goldbeter and Koshland [5]. The essential difference between Eqs. (1a) and (1b) and the earlier models is the non-zero q_1 and q_2 , i.e. the reversibility of the separate and distinct phosphorylation and dephosphorylation processes.

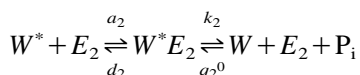
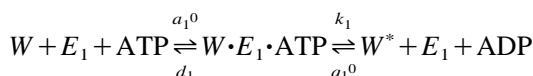
In order to carry out a cogent thermodynamic analysis for the kinetic model of PdPC, the reversibility of the biochemical reactions involved, specifically the phosphorylation catalyzed by kinase and dephosphorylation catalyzed by phosphatase, must be enforced. While this was known to be an important issue [13], almost all current models neglect the slow reverse steps.

2. Basic biochemical equilibrium and energetics

We consider a phosphorylation–dephosphorylation cycle (PdPC) catalyzed by kinase E_1 and phosphatase E_2 , respectively. The phosphorylation covalently modifies the protein W to become W^* :



It is important to note that Eq. (1a) is not the reverse reaction of Eq. (1b). In fact, recognizing the hydrolysis reaction $ATP \rightleftharpoons ADP + P_i$ explicitly, we have



Thus, at constant concentrations for ATP, ADP and P_i ,

$$a_1 = a_1^0[ATP], \quad q_1 = q_1^0[ADP], \quad q_2 = q_2^0[P_i] \quad (2)$$

For simplicity, we have assumed that these rate constants are pseudo-first order, which implies that ATP, ADP and P_i are sufficiently below the saturation levels for their respective enzymes.

The equilibrium constant for ATP hydrolysis therefore is

$$\frac{[ATP]_{eq}}{[ATP]_{eq}[P_i]_{eq}} = \frac{d_1 q_1^0 d_2 q_2^0}{a_1^0 k_1 a_2 k_2} = e^{-\Delta G^0/RT} \quad (3)$$

where ΔG^0 is the standard free-energy change for ATP hydrolysis reaction [14]. That is $(a_1 k_1 a_2 k_2)/(d_1 q_1 d_2 q_2) = 1$ in equilibrium. However, with physiological concentrations for ATP, ADP and P_i inside cells, the quotient

$$\gamma = \frac{a_1 k_1 a_2 k_2}{d_1 q_1 d_2 q_2} = \frac{a_1^0 k_1 a_2 k_2}{d_1 q_1^0 d_2 q_2^0} \left(\frac{[ATP]}{[ADP][P_i]} \right) \quad (4)$$

is directly related to the intracellular phosphorylation potential

$$RT \ln \gamma = \Delta G^0 + RT \ln \frac{[ATP]}{[ADP][P_i]} = \Delta G \quad (5)$$

where $RT = 0.6$ kcal/mol at room temperature. We shall also introduce an equilibrium constant for the dephosphorylation reaction catalyzed by phosphatase under intracellular phosphate concentration:

$$\mu = \frac{d_2 q_2}{k_2 a_2} \quad (6)$$

The two parameters γ and μ are the key augmentations to the model of Goldbeter and Koshland [5].

We recognize the fact that there is currently no experimental evidence for Eq. (1b) being reversible. While the backward rate for the dephosphorylation reaction catalyzed by a phosphatase can be extremely small, a thermodynamically correct model has to have a non-zero q_2^0 , no matter how small it is. In fact, Eq. (4) could be used to estimate the unmeasurable q_2^0 if all the other rate constants are known.

3. Reversible kinetic model for covalent modification

The kinetic equations for the reaction cycle in Eqs. (1a) and (1b) are straight-forward

$$\frac{d[W]}{dt} = -a_1[W] \times [E_1] + d_1[WE_1] + k_2[W^*E_1] - q_2[W][E_2]$$

$$\frac{d[WE_1]}{dt} = a_1[W][E_1] + (d_1 + k_1)[WE_1] + q_1[W^*][E_1]$$

$$\frac{d[W^*]}{dt} = -a_2[W^*] \times [E_2] + d_2[W^*E_2] + k_1[WE_1] - q_1[W^*][E_1]$$

$$\frac{d[W^*E_2]}{dt} = a_2[W^*][E_2] - (d_2 + k_2)[W^*E_2] + q_2[W][E_2] \quad (7)$$

These equations are solved in conjunction with conservation Eqs. (8)–(10):

$$W_T = [W] + [W^*] + [WE_1] + [W^*E_2] \quad (8)$$

$$E_{1T} = [E_1] + [WE_1] \quad (9)$$

$$E_{2T} = [E_2] + [W^*E_2] \quad (10)$$

Following the elegant mathematical treatment given in [5], we have the steady state fraction of phosphorylated W , denoted by $W^* = [W^*]/W_T$ as in [5], satisfying

$$\sigma = \frac{\mu\gamma[\mu - (\mu + 1)W^*](W^* - K_1 - 1)}{[\mu\gamma - (\mu\gamma + 1)W^*](W^* + K_2)} \quad (11)$$

Here, we have denoted

$$\sigma = \frac{k_1 E_{1T}}{k_2 E_{2T}}, \quad K_1 = \frac{d_1 + k_1}{a_1 W_T}, \quad K_2 = \frac{d_2 + k_2}{a_2 W_T}$$

These three parameters are in the original model

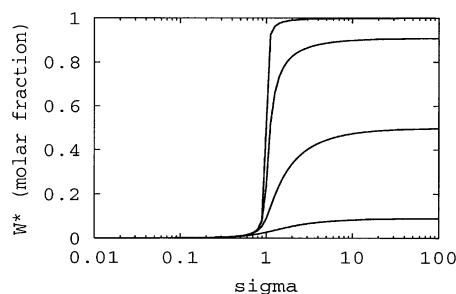


Fig. 1. Amplified sensitivity of a phosphorylation–dephosphorylation cycle as a function of intracellular phosphorylation potential ΔG . From top to bottom, $\gamma = 10^{10}$, 10^4 , 10^3 and 10^2 , corresponding to $\Delta G = 13.8$, 5.5, 4.1 and 2.8 kcal/mol. A value of 13.8 kcal/mol is typical for the intracellular phosphorylation potential [14,15]. Other parameters used in the computation: $K_1 = K_2 = 0.01$ and $\mu = 0.001$.

[5] which, by assuming *irreversible* reactions with $q_1 = q_2 = 0$, has $\mu = 0$ and $\gamma = \infty$. The value of σ represents the ratio of kinase activity to phosphatase activity. Hence, it characterizes the magnitude of the stimuli for the PdPC. $1/K_1$ and $1/K_2$ are the ratios of substrate concentrations to the Michaelis–Menten constants of kinase and phosphatase, respectively. A small K ($\ll 1$) means the enzymatic reaction is highly saturated.

More explicitly, Eq. (11) is a quadratic equation for W^* :

$$AW^{*2} - BW^* + C = 0 \quad (12)$$

in which

$$A = 1 + \mu - \sigma(1 + 1/\gamma\mu)$$

$$B = \mu + (1 + \mu)(1 + K_1) - \sigma(1 - K_2(1 + 1/\gamma\mu))$$

$$C = \mu(1 + K_1) + \sigma K_2$$

The steady state solution to Eq. (7) is therefore the positive root of Eq. (12)

$$W^* = \frac{B - \sqrt{B^2 - 4AC}}{2A} \quad (13)$$

It is plotted in Fig. 1 using $K_1 = K_2 = 0.01$, i.e.

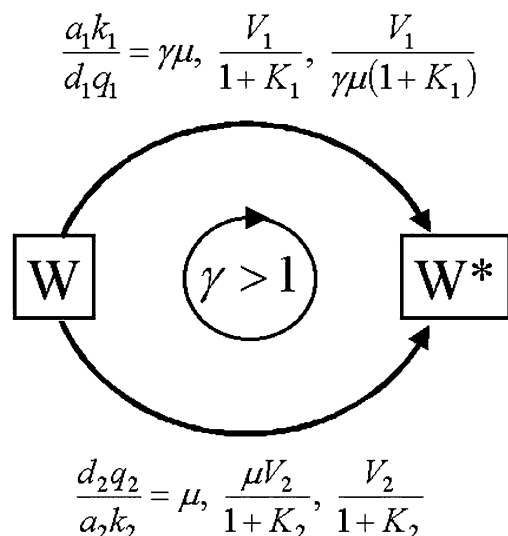


Fig. 2. A semi-quantitative, Michaelis–Menten, representation for the PdPC. The three numbers from each pathway correspond to the equilibrium constant, forward and backward rates for the enzymatic reaction. They satisfy their respective Haldane relationship for thermodynamic reversibility. In general, the steady-state $[W^*]/[W]$ is between μ and $\gamma\mu$. If $V_1 \gg V_2$, then it is near $\gamma\mu$, and if $V_2 \gg V_1$, it is near μ . When $\gamma > 1$, PdPC runs clockwise.

both enzymes are highly saturated and thus the rates are only weakly dependent on the respective substrate concentrations [5], and $\mu = 10^{-3}$, i.e. the dephosphorylation reaction is highly irreversible [13]. It is seen that the quality of the amplifier is directly related to the phosphorylation potential. In fact, when $\gamma = 1$, i.e. $\text{ATP} \rightleftharpoons \text{ADP} + \text{P}_i$ are in chemical equilibrium,

$$W^* = \frac{a_1 k_1}{a_1 k_1 + d_1 q_1} = \frac{d_2 q_2}{a_2 k_2 + d_2 q_2} = \frac{\mu}{1 + \mu} \quad (14)$$

which is independent of σ . In this case, the amplification is completely abolished. Biological amplification needs energy, just like a home stereo!

The switch-like behavior in Fig. 1 can be understood semi-quantitatively as follows (Fig. 2). The kinase catalyzed phosphorylation reaction has a Michaelis–Menten constant $K_1 W_T$ and $V_{\max} = V_1 = k_1 E_{1T}$. Therefore, the overall rate of the reaction is $V_1 / (1 + K_1)$; similarly, the dephosphorylation reaction has a rate $V_2 / (1 + K_2)$ where $V_2 = k_2 E_{2T}$. The

equilibrium constants for the respective reactions are $\mu\gamma = a_1 k_1 / d_1 q_1$ and $\mu = d_2 q_2 / a_2 k_2$. When $K_1 = K_2$ and $\sigma = V_1 / V_2 \gg 1$, the phosphorylation pathway is dominant. Hence, $[W^*]/[W] = \mu\gamma$. When $\sigma \ll 1$, the pathway is dominated by dephosphorylation and $[W^*]/[W] = \mu$. Therefore, for a finite γ , one does not expect $W^* \rightarrow 1$ as $\sigma \rightarrow \infty$, as clearly pointed out earlier in Gresser [13]. Rather, we have $W^* \rightarrow \mu\gamma / (1 + \mu\gamma)$ as $\sigma \rightarrow \infty$. For $\gamma = 10^3$ and $\gamma = 10^2, 10^3, 10^4$ and 10^{10} , the plateau of W^* towards the right in Fig. 1 is expected to be 0.099, 1/2, 10/11 and almost 1.

The response coefficient, R_v , which characterizes the steepness of the transition in covalent modification, has been defined as the ratio of σ when $W^* = 90\%$ to the σ when $W^* = 10\%$ [5]. For a simple Michaelis–Menten kinetics its value is 81. A value of 1 means the transition is infinitely steep. With finite γ and μ , in theory, because W^* never exceeds 0.9 for a range of μ and γ (Fig. 1), R_v needs to be redefined as the ratio of σ when $W^* = 0.9W^*(\infty) + 0.1W^*(-\infty)$ to σ when $W^* = 0.9W^*(-\infty) + 0.1W^*(\infty)$, where $W^*(\infty) = \mu\gamma / (1 + \mu\gamma)$ and $W^*(-\infty) = \mu / (1 + \mu)$. In physiological reality, $W^*(\infty) > 0.9$ and $W^*(-\infty) < 0.1$; that is $\mu < 1/9$ and $\mu\gamma > 9$. Fig. 3 shows how the response coefficient,

$$R_v = \frac{(\mu - 9)(9\mu\gamma - 1)(K_1 + 0.1)(K_2 + 0.1)}{(\mu\gamma - 9)(9\mu - 1)(K_1 + 0.9)(K_2 + 0.9)} \quad (15)$$

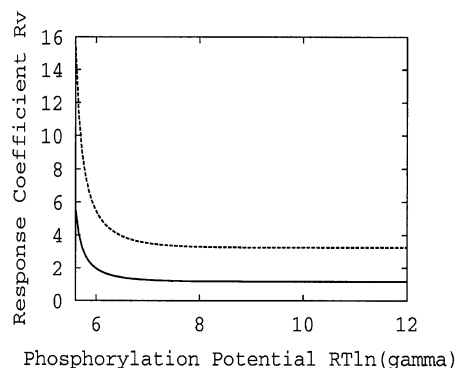


Fig. 3. Intracellular phosphorylation potential, $\Delta G = RT \ln \gamma$ (kcal/mol) controls the sensitivity amplification of a PdPC. The response coefficient R_v is defined as $\sigma(W^* = 0.9) / \sigma(W^* = 0.1)$ in Fig. 1 [5]. The solid line is for $K_1 = K_2 = 0.01$, and the dashed line for $K_1 = K_2 = 0.1$. Both with $\mu = 10^{-3}$.

depends on the phosphorylation potential $\Delta G = RT \ln \gamma$. It is seen that for the physiological range of ΔG , the steepness R_v reaches its minimal, plateau value given in Goldbeter and Koshland [5].

The current model in fact makes a prediction. Let $W^*(-\infty)$ and $W^*(\infty)$ be the left and right plateaus of the amplification curve in Fig. 1, which are very close to 0 and 1, respectively. Then

$$\frac{W^*(-\infty)}{1-W^*(\infty)} \approx \frac{W^*(-\infty)}{1-W^*(-\infty)} \times \frac{W^*(\infty)}{1-W^*(\infty)} = \frac{1}{\mu} \times \mu \gamma = \gamma \quad (16)$$

In contrast, the previous model [5] predicts an indeterminate 0/0.

The steepness of the curves in Fig. 1 can also be characterized by the slope at its mid-point, known as the Hill coefficient in the theory of allosteric cooperativity [14]. It can be obtained analytically from Eq. (11):

$$n_v = \left(\frac{dW^*}{d \ln \sigma} \right)_{W^*=0.5} \approx \frac{1}{4} \times \left(\mu + \frac{1}{\mu \gamma} + K_1 + K_2 \right)^{-1} \quad (17)$$

when K_1 , K_2 and μ are small and $\mu \gamma$ is large. We see again that the steepness increases with increasing γ .

4. Temporal cooperativity

Allosteric change in and covalent modification of proteins are two most basic phenomena in cellular signaling processes [6]. While the equilibrium thermodynamic principle of the former is well understood [16], relatively little attention has been given to the non-equilibrium steady-state thermodynamics [17] of the latter. The analysis developed in the present paper indicates that the cooperativity in the cyclic reaction is temporal, with energy ‘stored’ in time rather than in space as for allosteric cooperativity. This concept is similar to the *energy relay* which was first pro-

posed by Hopfield for understanding the molecular mechanism of kinetic proofreading in protein synthesis [18,19]. We now elaborate on this concept by carrying out a quantitative comparison between the steady state system given in Eqs. (1a) and (1b) and allosteric cooperativity.

4.1. High-order vs. zero-order reactions

One of the most fundamental differences between allosteric cooperativity and zero-order ultra-sensitivity is apparently the order of the reactions. Allosteric cooperativity is based on a reaction with high-order



where K is the equilibrium constant for protein P binding single-ligand L . The corresponding fraction of protein with ligand then is

$$Y = \frac{[PL_n]}{[P] + [PL_n]} = \frac{(KL)^n}{1 + (KL)^n} \quad (19)$$

Eq. (19) indicates that the steepness of the curve Y vs. $\ln(K[L])$ increases with n . On the other hand, ultrasensitivity is based on both phosphorylation and dephosphorylation reactions being enzyme limited; hence, both have a very weak dependence on the respective substrate concentrations $[W]$ and $[W^*]$. In the steady state

$$k_{ph}[W]^\nu = k_{dp}[W^*]^\nu \quad (20)$$

where k_{ph} and k_{dp} are the rates of phosphorylation and dephosphorylation, and ν , the ‘order of the reaction’, is near zero. (Normally the power term to the concentration of a species implies the stoichiometry of that species in a reaction. The meaning of ν here is that the reaction is even less than first-order. Both a hyperbolic curve, as expected from an enzymatic reaction with saturation, and a curve with power $\nu < 1$ are concave down with negative curvature.) The corresponding fraction of protein in the activated state

$$Z = \frac{[W^*]}{[W] + [W^*]} = \frac{k_{ph}^{1/\nu}}{k_{ph}^{1/\nu} + k_{dp}^{1/\nu}} \quad (21)$$

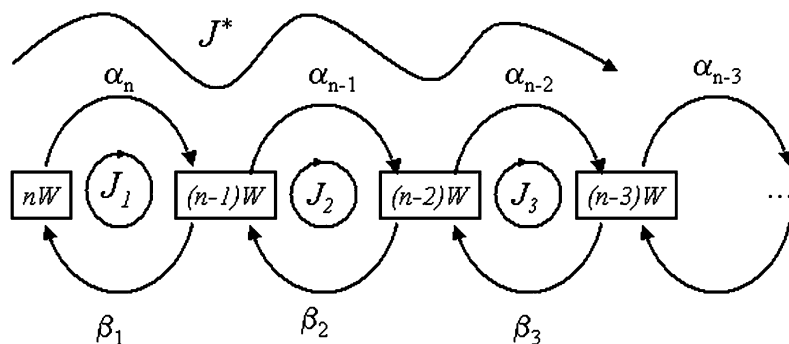


Fig. 4. Detailed kinetic scheme showing how the PdPCs are being completed while nW molecules are transformed to W^* . The 'futile' cycles are indicated by J_1, J_2 , etc., and the net flux for W^* formation is denoted by J^* . According to Michaelis–Menten kinetics, transition rates $\alpha_i = k_1 E_{1T}/1 + (nK_1/i)$ and $\beta_j = k_2 E_{2T}/1 + (nK_2/j)$, which are weakly substrate-dependent when K values are small. $\alpha_i/\beta_j \neq i\alpha_1/j\beta_1$ means cooperativity. The process is closely related to a biased random walk with J^* and J_k analogous to the 'drift velocity' and 'diffusion constant', respectively.

Eq. (21) indicates that the steepness of the curve Z vs. $\ln(k_{ph}/k_{dp})$ increases with $1/\nu$. Therefore, the optimal situation is a zero-order reaction with $\nu = 0$.

Surprisingly, allosteric binding (Eq. (18)) can yield an equation identical to Eq. (20). Let the equilibrium constant $K = k_+/k_-$ where k_+ and k_- are association and dissociation rate constants. Then, in the equilibrium $(k_+[L])^n[P] = k_-[PL_n]$. That is

$$k_+[L][P]^{1/n} = k_-[PL_n]^{1/n} \quad (22)$$

4.2. Temporal cooperativity in zero-order reaction cycle

The cooperativity achieved by ultrasensitivity can therefore be stated as follows. It takes on average, $n_v = 1/\nu$ PdPCs in order to transform one W to W^* . There is a temporal cooperativity on the scale of n_v cycles. Therefore, n_v in time is analogous to the number of subunits in allosteric cooperativity (see Eqs. (20) and (22)). Most importantly, transforming one W to one W^* through multiple 'futile' cycles is precisely the mechanism proposed by Hopfield for kinetic proofreading of protein biosynthesis (with branched reaction pathways) in which $n_v \approx 2$ [18,19]. Multiple branched pathways have been proposed for kinetic proofreading in T-cell receptor signaling [20]. Of course,

the ATP hydrolysis is not futile, rather the energy supplies the need to maintain high accuracy and sensitivity or improved memory of a steady-state 'living' system away from true thermodynamic equilibrium.

The above statement can be further quantified. Let us consider a system with only a single E_1 and a single E_2 molecule, but nW substrate molecules. The complete kinetics of W^* formation can be represented by a chain kinetic scheme shown in Fig. 4 [21], which is a detailed version of what is shown in Eqs. (1a) and (1b). Each time when a cycle is completed, one ATP molecule is hydrolyzed. The cooperativity of the kinetics in Fig. 4 is characterized by

$$\frac{\alpha_{n-i}}{\beta_{i+1}} \left[\frac{(n-i)\alpha_1}{(i+1)\beta_1} \right]^{-1} = \frac{i+1+nK_2}{n-i+nK_1} \quad (23)$$

For n completely independent W molecules undergoing $W \rightleftharpoons W^*$ transition, Eq. (23) is expected to be unity. However, the nW molecules in Fig. 4 are not independent since they are linked by the enzymatic reactions. For small K_1 and K_2 , there is cooperative phosphorylation when $i > n/2$ and there is cooperative dephosphorylation when $i < n/2$.

Fig. 5 shows the steepness of the response curve for the model given in Fig. 4. The detailed model

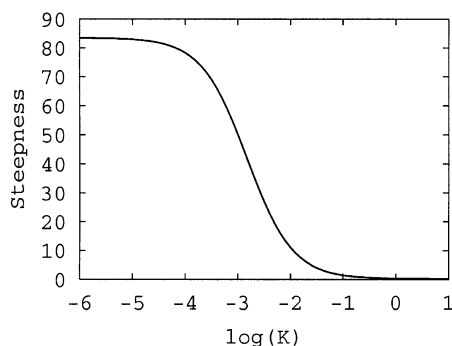


Fig. 5. The steepness n_v according to the kinetic model in Fig. 4. Firstly, $[W^*]/[W] + [W^*]$ is calculated as a function of $\ln(k_1/k_2)$ where $K_1 = K_2 = K$. The steepness, n_v , of the curve is the slope at its mid-point. Other parameters used: $E_{1T} = E_{2T} = 1$, $n = 1000$. It can be analytically shown that for small K , $n_v = (n+2)/12 = 83.5$, and for large K , $n_v = 1/4$. For $K = 0.01$, $n_v \approx 12.5$ according to Eq. (17).

gives the same $n_v = 12.5$ for $K_1 = K_2 = 0.01$. The significance of this chain model, however, is that it reveals the origin of the cooperativity [22]. Furthermore, according to the theory of linear cooperativity [23,22], the steepness of the curves in Fig. 1 is directly related to the microscopic fluctuation in the number of W^* .

Fig. 6 shows a numerical example of the reaction kinetics of the model given in Fig. 4. The large fluctuations in the number of W^* molecules is directly related to n_v . In fact, $\sqrt{\langle(\Delta W^*)^2\rangle} = \sqrt{nm_v}$ is expected to be 112. A more cooperative system has larger fluctuations.

5. Discussion

The rigorous thermodynamic analysis of the model for the phosphorylation–dephosphorylation cycle (PdPC) originally proposed in Refs. [4,5] indicates that sustained intracellular phosphorylation potential is essential in the functioning of the signal transduction process. This result suggests that the ubiquitous phosphorylation in biological signaling processes, in addition to the covalent chemical modification which leads to structural recognition, also utilizes biochemical energy from the high-energy phosphate in order to carry out its function with high accuracy, robustness, sensitivity,

and specificity [18,11,24]. The analysis also reveals a shared mechanism between the ultrasensitivity and kinetic proofreading in a large class of cellular processes involving GTPases [12]. Both use cycle kinetics [17] to improve the power of biological selectivity.

Our quantitative analysis also provided a clear mechanistic origin for the high cooperativity in the zero-order ultrasensitivity. A chain kinetic model indicates that the cooperativity is achieved through temporal cooperativity. This mechanism is parallel in mathematical form to, but fundamentally different in biochemical nature from, the allo-

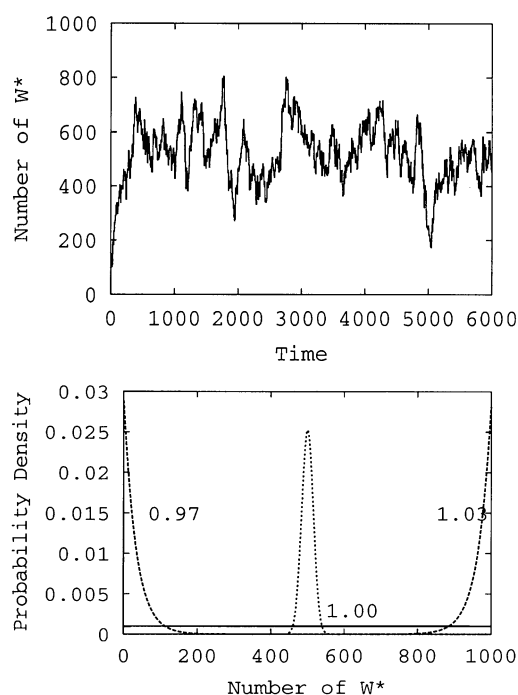


Fig. 6. Upper panel shows a numerical simulation of the reaction given in Fig. 4, with $n = 1000$, $E_{1T} = E_{2T} = 1$, $K_1 = K_2 = 0.01$, $k_1 = k_2 = 100$. Since $\sigma = 1$, the steady state value of $[W^*] = 500$. The large fluctuations in the number of W^* molecules is directly related to n_v : $\sqrt{\langle(\Delta W^*)^2\rangle} = \sqrt{nm_v}$. The lower panel shows the probability distributions for the number of W^* . Solid flat line, $\sigma = 1.00$; dashed lines, different distributions for $\sigma = 0.97$ and 1.03 , respectively. We see a sharp response to σ being less and greater than 1. In comparison, the central peak with dotted line is for a non-cooperative system with 1000 independent molecules and $\sigma = 1$. A more cooperative system has larger fluctuations.

steric cooperativity of multi-subunits protein systems [16]. Both temporal and allosteric cooperativities have a deep connection to the molecular fluctuations as shown in Fig. 6 [21], an insight largely unexplored in the studies of biological signal transduction processes.

In order to compare our result with that of Goldbeter and Koshland, we have used the value $K_1 = K_2 = 0.01$ in this study. These values are extreme cases and many PdPCs studied in laboratory experiments show much less cooperativity. With $K_m \approx 0.1$ – $1 \mu\text{M}$ and concentrations of $\sim 1 \mu\text{M}$ for the kinases in the MAPK pathway [8], the realistic value will be ~ 0.1 – 1 . The phosphatase concentration is even lower, $\sim 1 \text{ nM}$. Note that from Eq. (17) high cooperativity requires both K_s for the kinase and the phosphatase to be small. The current model analysis also suggests that the source of phosphate in a PdPC, while chemically equivalent, could be important. A phosphate from ATP hydrolysis can be energetically different from a phosphate from GTP hydrolysis. In the cells, $[\text{ATP}] \sim 10 \text{ mM}$, $[\text{ADP}] \sim 10 \mu\text{M}$, $[\text{GTP}] \sim 1 \text{ mM}$, $[\text{GDP}] \sim 100 \mu\text{M}$, and $[\text{Pi}] \sim 1 \text{ mM}$ [15]. Therefore, different cellular biochemical ‘batteries’ can have different ‘voltages’.

Acknowledgments

Professor Walter Kauzmann’s work on the physical chemistry of hydrophobic interactions in proteins was an important part of my post-doctoral education with John Schellman. In the present work, I try to follow the same spirit of that work by raising a basic physicochemical question about a currently important biological problem: is there a thermodynamic role for the prevalent phosphorylation in biological signal transduction processes? I thank Jon Cooper, Eddy Fischer, Bob Franza, John Hopfield, Guangpu Li, and Elliott Ross for helpful discussions, and Jim Bassingthwaite and P. Boon Chock for carefully reading of this manuscript.

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